### **MASSIVE MIMO: FUNDAMENTALS AND SYSTEM ISSUES**

Thomas L. Marzetta Bell Labs, Alcatel-Lucent

Lund Circuit Design Workshop

23 September, 2015

You can always lay down more optical fiber; you can never lay down more spectrum!



### SPECTRUM BELOW 5 GHZ: THE MOST VALUABLE RESOURCE IN THE WORLD!

- FCC AWS-3 spectrum auction, January 2015
  - 65 MHz: 1695-1710 MHz, 1755-1780 MHz, 2155-2180 MHz
  - \$41.3 billion



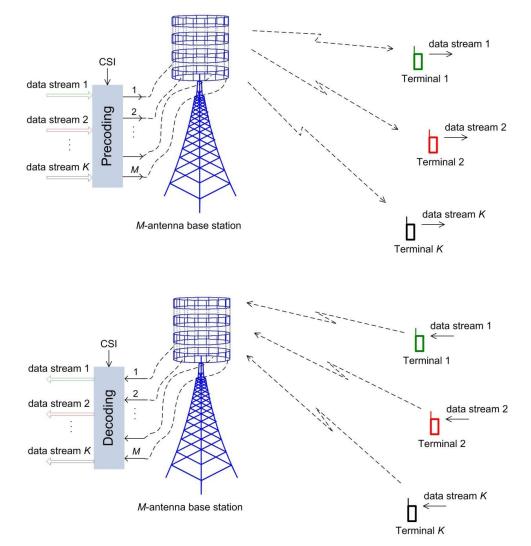
### SPECTRUM BELOW 5 GHZ: THE MOST VALUABLE RESOURCE IN THE WORLD!

- FCC AWS-3 spectrum auction, January 2015
  - 65 MHz: 1695-1710 MHz, 1755-1780 MHz, 2155-2180 MHz
  - \$41.3 billion
- FCC Commissioner Jessica Rosenworcel, October 2, 2014:
- "What if we issued a challenge in Washington? ... Imagine that we decided to reward the first person who finds a way to make spectrum use below 5 GHz 50 or 100 times more efficient over the next decade. The reward could be something simple—say 10 megahertz of spectrum suitable for mobile broadband."

#### Only advancements in the physical layer can meet this challenge



### SPATIAL MULTIPLEXING PUSHED TO AN EXTREME



#### Massive MIMO serves all users over the *same* time/frequency resources

4 COPYRIGHT © 2015 ALCATEL-LUCENT. ALL RIGHTS RESERVED. ·Bell Labs 🕖

### WHAT IS MASSIVE MIMO?

- Essentials
  - many physically small, low power antennas
  - aggressive spatial multiplexing
  - utilize *measured* channels
- Benefits
  - scalability
  - spectral efficiency
  - simplicity
  - great service to all users
  - energy efficiency

#### Massive MIMO is a game-changer

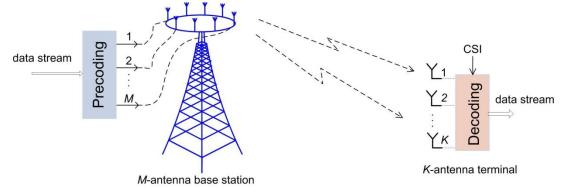


### OUTLINE

- Information theoretic evolution of MIMO
- Science of Massive MIMO
- Case study
  - Optimum pilot re-use
  - Maximum-ratio vs. zero-forcing



#### POINT-TO-POINT MIMO PAULRAJ & KAILATH (1993); FOSCHINI (1995); RALEIGH & CIOFFI (1998)



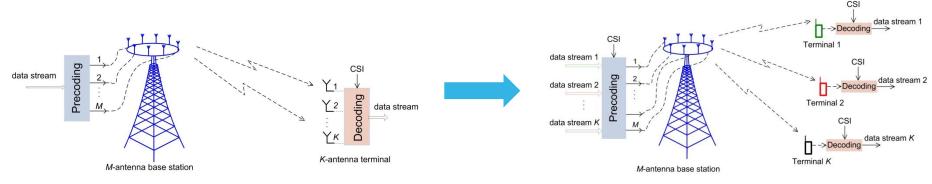
- Brilliant invention
- But not scalable
  - unfavorable propagation
  - time required for training grows with system size
  - disappointing multiplexing gains at cell edges
  - 8x4 link, -3.0 dB SNR:

# base station antennas	1	2	4	8
bits/second/Hz	1.51	1.83	2.06	2.19

It's critically important to give uniformly good service throughout the cell

### **MULTI-USER MIMO**

CAIRE & SHAMAI (2003); VISWANATH & TSE (2003); VISHWANATH, JINDAL, & GOLDSMITH (2003)

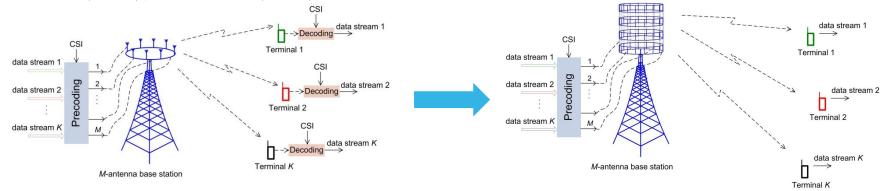


- Splitting the multi-antenna user into autonomous singleantenna users doesn't decrease the sum-throughput!
- Only single-antenna terminals required
- Propagation is almost always favorable
- But not scalable in its original form
  - dirty-paper coding/decoding needed
  - both ends of link have to know channel

A triumph of Shannon information theory, but not really practical as is

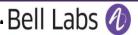


#### MASSIVE MIMO MARZETTA (2006); MARZETTA (2010)



- Add many more base station antennas
- Ignore the dictates of Shannon theory
  - channel state information (CSI) only available to the base station
  - use linear pre-coding/de-coding instead of dirty-paper
  - users don't do any signal processing

The large number of antennas paradoxically makes the problem simpler



### MASSIVE MIMO: MORE THAN JUST MANY ANTENNAS

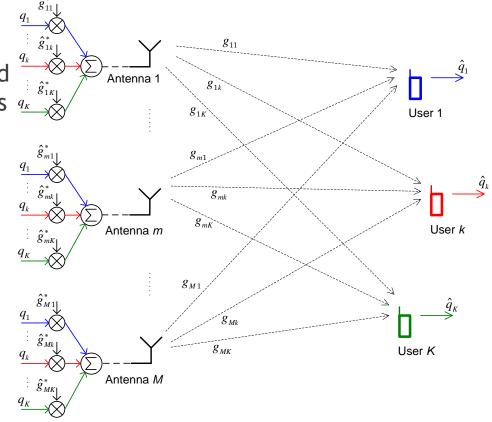
- Using *measured* channels: Beamforming gain grows linearly with number of antennas, irrespective of the noisiness of the measurements
- Frequency-independent power control: Based solely on long-scale (slow) fading, is exceedingly effective
- Pilot contamination: Ultimate limitation in non-cooperative multi-cell systems

#### No new mathematics, but a new philosophy!

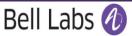


#### DOWNLINK DATA TRANSMISSION: CONJUGATE BEAMFORMING ANTENNAS TRANSMIT THE WEIGHTED MESSAGE-BEARING SYMBOLS TO ARRIVE IN-PHASE AT THE INTENDED USER & OUT-OF-PHASE ELSEWHERE

- Information-bearing symbols combined with *measured* channel characteristics  $q_{\kappa}$ to create transmitted signals
- Decentralized array architecture

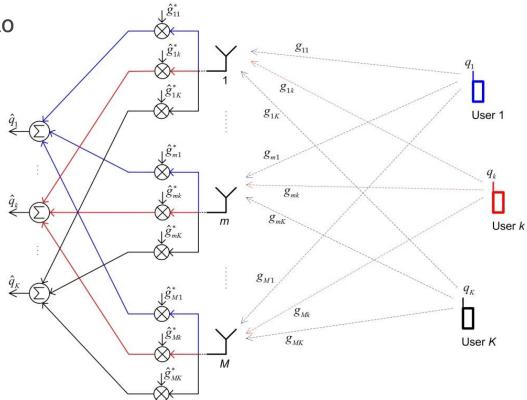


#### The simplest possible pre-coding, but often very effective



#### UPLINK DATA TRANSMISSION: MATCHED FILTERING BASE STATION WEIGHTS AND ADDS RECEIVED SIGNALS FOR CONSTRUCTIVE REINFORCEMENT OF THE TRANSMISSION FROM EACH USER

• Properties and advantages similar to conjugate beamforming

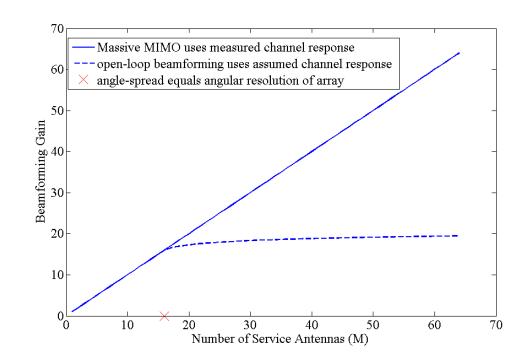


For high SINRs, zero-forcing may outperform conjugate beamforming/matched-filtering



# WHY SO IMPORTANT TO DO BEAMFORMING WITH *MEASURED* PROPAGATION?

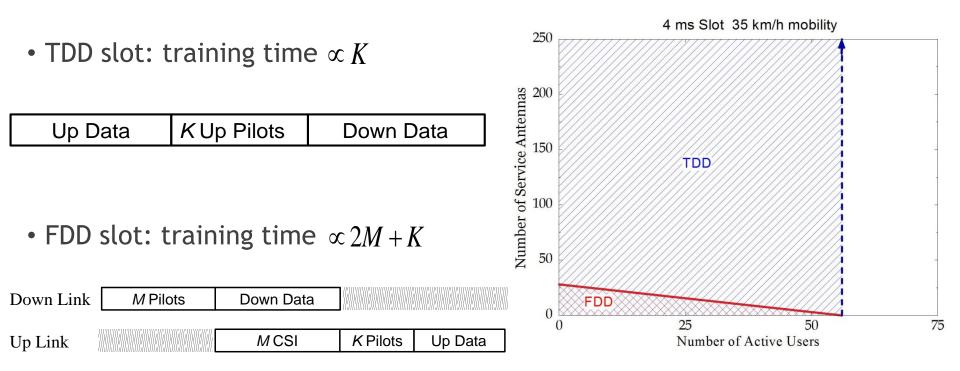
- Measured channels
  - scalable
  - gain grows linearly with number of antennas
    - irrespective of noisiness of CSI
    - no tightening of array tolerance required
- Assumed channels
  - not scalable
  - gain eventually grows only logarithmically



#### If open-loop beamforming, then not Massive MIMO!



### TDD SLOT STRUCTURE ENSURES TIMELY CHANNEL-STATE INFORMATION: M SERVICE-ANTENNAS, K USERS



Mobility limits the number of active users; FDD is a disaster!

•Bell Labs 🕢

COPYRIGHT © 2015 ALCATEL-LUCENT. ALL RIGHTS RESERVED.

14

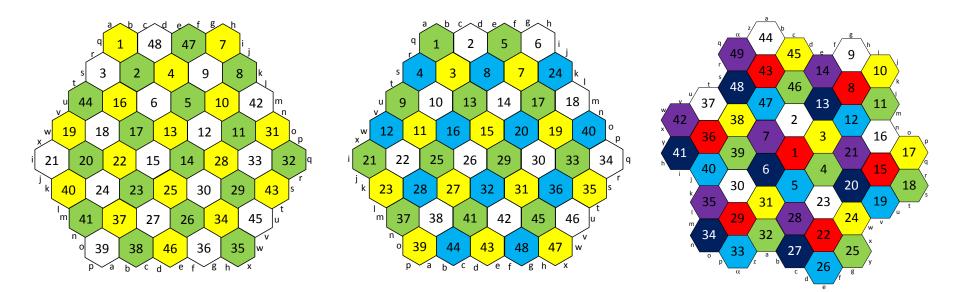
# PILOT CONTAMINATION

- For mobile users, there is a limited number of orthogonal pilots
- When the same pilot is transmitted by more than one user:
  - base station obtains a *linear combination* of channels
    - extra pilot power doesn't help
  - coherent interference
    - doesn't disappear with more antennas

#### Pilot contamination has always existed, but was never noticed!



# PILOT RE-USE FACTOR 3, 4, 7: PUSH CONTAMINATING CELLS FARTHER AWAY FROM HOME CELL



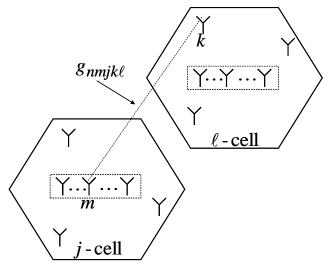
#### The cost: extra overhead



COPYRIGHT © 2015 ALCATEL-LUCENT. ALL RIGHTS RESERVED.

16

# •**Propagation Model** $g_{mk} = \underbrace{\beta_k^{1/2}}_{\text{slow}} \cdot \underbrace{h_{mk}}_{\text{fast}}, m: \text{ antenna } k: \text{ terminal}$



Bell Lat

- Slow fading and fast fading
- Slow fading comprises geometric attenuation (Hata Model) combined with log-normal shadow fading
  - Constant with respect to frequency and service antenna
  - Easy to estimate
  - Assumed known a-priori
- Fast fading
  - Rayleigh CN(0,1), iid with respect to antenna, terminal
  - Piecewise constant and iid from one frequency smoothness interval to another
  - Unknown a-priori
  - Estimated from up link pilots & TDD reciprocity

### DOWN LINK DATA: LINEAR PRE-CODING

$$M \times 1 \qquad M \times K \overbrace{\mathbf{D}_{\eta}^{1/2}}^{K \times 1} K \times 1$$
  
$$\widehat{\mathbf{s}} = \widehat{\mathbf{A}} \widehat{\mathbf{D}_{\eta}^{1/2}} \widehat{\mathbf{q}}$$
  
$$\{q_k\}: \text{iid}, \text{CN}(0,1) \qquad E\left\{\mathbf{s}^{\text{H}}\mathbf{s}\right\} = 1 \qquad \text{power-control}: \eta \ge \mathbf{0}, \mathbf{1}^{\text{T}} \eta = 1$$

- Conjugate beam-forming

$$\mathbf{A} = \frac{1}{\sqrt{M}} \hat{\mathbf{G}}^* \mathbf{D}_{\gamma}^{-1/2}$$

- permits de-centralized architecture and processing - Zero-forcing  $\mathbf{A} = \sqrt{M - K} \hat{\mathbf{G}}^* (\hat{\mathbf{G}}^T \hat{\mathbf{G}}^*)^{-1} \mathbf{D}_{\gamma}^{1/2}$ 

- Implementing linear pre-coding takes more computations than QR factorization!

DOWN LINK: CONJUGATE BEAM-FORMING  

$$\mathbf{x} = \sqrt{\frac{\rho_{\mathrm{f}}}{M}} \mathbf{G}^{\mathrm{T}} \hat{\mathbf{G}}^{*} \mathbf{D}_{\gamma}^{-1/2} \mathbf{D}_{\eta}^{1/2} \mathbf{q} + \mathbf{w} = \sqrt{\frac{\rho_{\mathrm{f}}}{M}} \hat{\mathbf{G}}^{\mathrm{T}} \hat{\mathbf{G}}^{*} \mathbf{D}_{\gamma}^{-1/2} \mathbf{D}_{\eta}^{1/2} \mathbf{q} + \mathbf{w} - \sqrt{\frac{\rho_{\mathrm{f}}}{M}} \hat{\mathbf{G}}^{\mathrm{T}} \hat{\mathbf{G}}^{*} \mathbf{D}_{\gamma}^{-1/2} \mathbf{D}_{\eta}^{1/2} \mathbf{q} + \mathbf{w} - \sqrt{\frac{\rho_{\mathrm{f}}}{M}} \hat{\mathbf{G}}^{*} \mathbf{D}_{\gamma}^{-1/2} \mathbf{D}_{\eta}^{1/2} \mathbf{q} + \hat{\mathbf{g}}_{k}^{\mathrm{T}} \sum_{n \neq k} \sqrt{\frac{\rho_{\mathrm{f}} \eta_{n}}{M \gamma_{n}}} \hat{\mathbf{g}}_{n}^{*} q_{n}$$

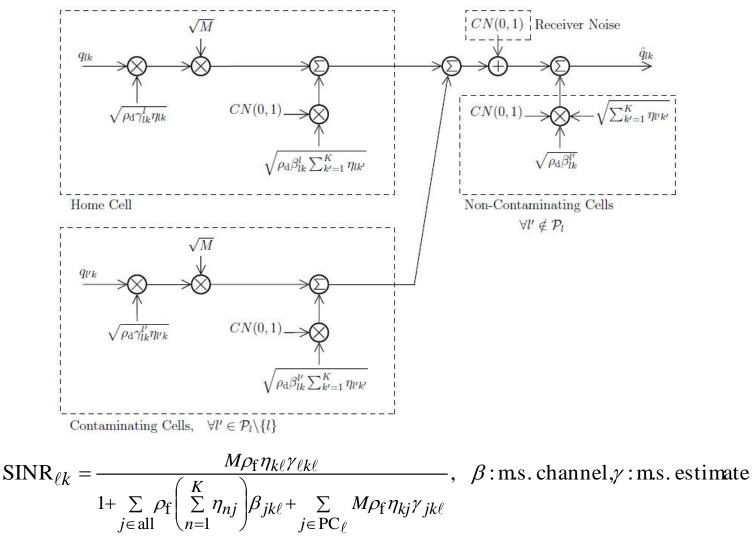
$$= \sqrt{\frac{\rho_{\mathrm{f}} \eta_{k}}{M \gamma_{k}}} \mathbf{E} \left\{ \hat{\mathbf{g}}_{k}^{\mathrm{T}} \hat{\mathbf{g}}_{k}^{*} \right\} \mathbf{q}_{k} + \frac{w_{k}}{(1)} - \sqrt{\frac{\rho_{\mathrm{f}}}{M}} \mathbf{g}_{k}^{\mathrm{T}} \hat{\mathbf{G}}^{*} \mathbf{D}_{\gamma}^{-1/2} \mathbf{D}_{\eta}^{1/2} \mathbf{q}$$

$$+ \frac{\hat{\mathbf{g}}_{k}^{\mathrm{T}} \sum_{n \neq k} \sqrt{\frac{\rho_{\mathrm{f}} \eta_{n}}{M \gamma_{n}}} \hat{\mathbf{g}}_{n}^{*} q_{n} + \sqrt{\frac{\rho_{\mathrm{f}} \eta_{k}}{M \gamma_{k}}} \left( \hat{\mathbf{g}}_{k}^{\mathrm{T}} \hat{\mathbf{g}}_{k}^{*} - \mathbf{E} \left( \hat{\mathbf{g}}_{k}^{\mathrm{T}} \hat{\mathbf{g}}_{k}^{*} \right) \right) \mathbf{q}_{k}$$
(4)

(0) desired signal	(1) receiver noise	(2) channel estimation error	(3) channel non- orthogonality	(4) beam- forming gain uncertainty
$M  ho_{ m f} \eta_k \gamma_k$	1	$\rho_{\rm f}(\beta_k-\gamma_k)$	$ \rho_{\mathrm{f}} \gamma_k \sum_{n \neq k} \eta_n $	$ \rho_{\mathrm{f}} \gamma_k \eta_k$

$$\operatorname{SINR}_{k} = \frac{\eta_{k} M \rho_{\mathrm{f}} \gamma_{k}}{1 + \rho_{\mathrm{f}} (\beta_{k} - \gamma_{k}) + \rho_{\mathrm{f}} \gamma_{k} \sum_{n \neq k} \eta_{n} + \rho_{\mathrm{f}} \gamma_{k} \eta_{k}} = \frac{\eta_{k} M \rho_{\mathrm{f}} \gamma_{k}}{1 + \rho_{\mathrm{f}} \left(\sum_{n=1}^{K} \eta_{n}\right) \beta_{k}}$$

#### **DOWNLINK MAXIMUM-RATIO: EFFECTIVE CHANNEL**



#### Massive MIMO creates a flat channel to each terminal



20

#### SINR FOR K-TH TERMINAL IN ELL-TH CELL

 $\beta$ : m.s. channel  $\gamma$ : m.s. estimate  $\beta - \gamma$ : m.s. error  $\eta$ : power control

	Conjugate Beam Forming / Matched Filtering	Zero Forcing
Down Link	$\frac{M\rho_{\rm f}\eta_{k\ell}\gamma_{\ell k\ell}}{1+\sum_{j\in{\rm all}}\rho_{\rm f}\left(\sum_{n=1}^{K}\eta_{nj}\right)\beta_{jk\ell}+\sum_{j\in{\rm PC}_{\ell}}M\rho_{\rm f}\eta_{kj}\gamma_{jk\ell}}$	$\frac{(M-K)\rho_{\mathrm{f}}\eta_{k\ell}\gamma_{\ell k\ell}}{1+\sum_{j\notin\ell\cup\mathrm{PC}_{\ell}}\rho_{\mathrm{f}}\left(\sum_{n=1}^{K}\eta_{nj}\right)\beta_{jk\ell}+\sum_{j\in\ell\cup\mathrm{PC}_{\ell}}\rho_{\mathrm{f}}\left(\sum_{n=1}^{K}\eta_{nj}\right)(\beta_{jk\ell}-\gamma_{jk\ell})+\sum_{j\in\mathrm{PC}_{\ell}}(M-K)\rho_{\mathrm{f}}\eta_{kj}\gamma_{jk\ell}}$
Up Link	$\frac{M\rho_{\mathrm{r}}\eta_{k\ell}\gamma_{\ell k\ell}}{1+\sum_{j\in\mathrm{all}}\rho_{\mathrm{r}}\sum_{n=1}^{K}\eta_{nj}\beta_{\ell nj}+\sum_{j\in\mathrm{PC}_{\ell}}M\rho_{\mathrm{r}}\eta_{kj}\gamma_{\ell kj}}$	$\frac{(M-K)\rho_{\mathrm{r}}\eta_{k\ell}\gamma_{\ell k\ell}}{1+\sum_{j\notin\ell\cup\mathrm{PC}_{\ell}}\rho_{\mathrm{r}}\sum_{n=1}^{K}\eta_{nj}\beta_{\ell nj}+\sum_{j\in\ell\cup\mathrm{PC}_{\ell}}\rho_{\mathrm{r}}\sum_{n=1}^{K}\eta_{nj}(\beta_{\ell nj}-\gamma_{\ell nj})+\sum_{j\in\mathrm{PC}_{\ell}}(M-K)\rho_{\mathrm{r}}\eta_{kj}\gamma_{\ell kj}}$

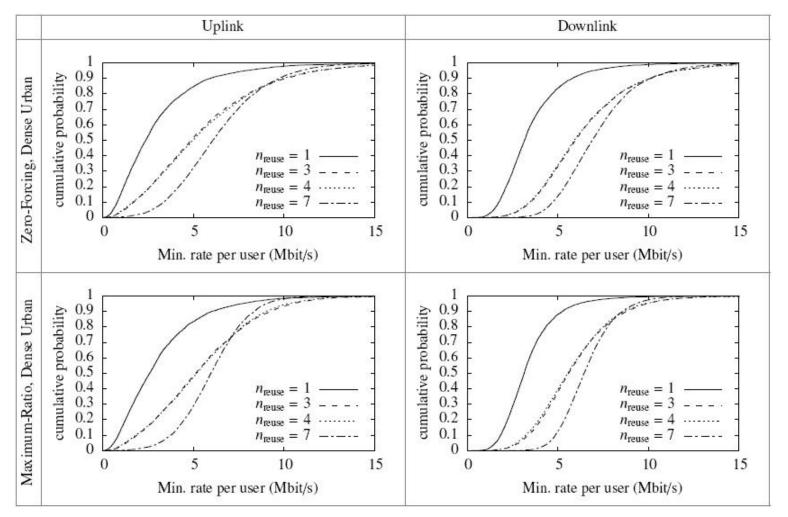
 Inequality constraints on SINR equivalent to linear inequality constraints on power control variables

### CASE STUDIES: OPTIMUM PILOT RE-USE FACTOR; MAXIMUM-RATIO VS. ZERO-FORCING

	Dense Urban	Suburban
Carrier frequency(GHz)	1.9	1.9
TDD spectral bandwidth (MHz)	20	20
Slot duration (ms)	2	1
User allowed mobility (km/h)	71	142
Uplink radiated power/user (mW)	200	200
Number of service antennas	64	256
Total downlink radiated power (W)	1	1
Active users/cell	18	18
Cell radius (km)	.50	2.0
Power control	Max/min	Max/min
95% likely throughput/terminal Mb/s zero-forcing	4.1 down, 2.6 up	3.1 down, 1.1 up
95% likely throughput/terminal Mb/s maximum-ratio	4.5 down, 3.1 up	3.2 down, 1.1 up

22 COPYRIGHT © 2015 ALCATEL-LUCENT. ALL RIGHTS RESERVED - Bell Labs 🕖

### NET THROUGHPUT PER USER: DENSE URBAN



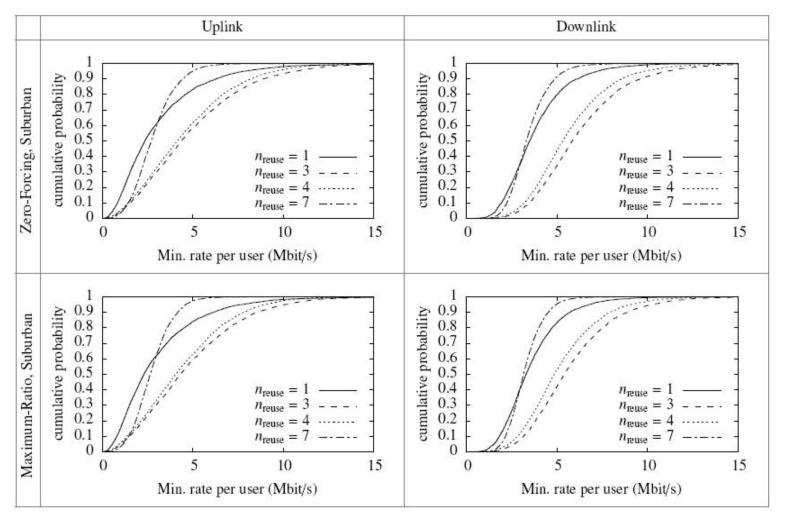
#### Maximum-ratio + pilot re-use 7 best for Dense Urban

COPYRIGHT © 2015 ALCATEL-LUCENT. ALL RIGHTS RESERVED.

23

·Bell Labs 🕢

#### NET THROUGHPUT PER USER: SUBURBAN



#### Maximum-ratio + pilot re-use 3 best for Suburban

COPYRIGHT © 2015 ALCATEL-LUCENT. ALL RIGHTS RESERVED.

24

•Bell Labs 💋

### NON-CELLULAR MASSIVE MIMO

- Backhaul for small-cells
- Cell-Free Massive MIMO
  - M randomly distributed access points serve K users over an entire city
- Fixed wireless access to homes
- Multicasting
  - Deliberately create and take advantage of pilot contamination!



### **MASSIVE MIMO IN NON-ELECTROMAGNETIC MEDIA**

- Hyperbolic
  - acoustic waves
  - elastic waves
- Parabolic
  - heat diffusion
- Eliptical
  - electric current: Ground Telegraphy (Richard Courant, Arnold Sommerfeld, Lee de Forest)



## MASSIVE SENSOR TELEMETRY

- Outstanding examples of signal processing
  - 3D reflection seismology
  - Computer tomography
  - Synthetic aperture radar
- Essential to sample data spatially and temporally at Nyquist rate
  - Proper sampling and huge data sets make physics-based signal processing easier!
- Uplink Massive MIMO transports data intact and in real time

#### Massive MIMO means more than entertainment enablement

